CRITERIA FOR USING A ONE-DIMENSIONAL HYDRODYNAMIC MODEL FOR TWO BARRAGES SITUATED IN MEDITERRANEAN REGION

Takkouk Saddek Maître Assistant, Université de Batna, Algérie *Xavier Casamitjana* Maître de conférence, Université de Girona, catalogne, Espagne

Abstract:

In order to characterise the barrage regime is usually very important to check the validity of assumptions on which its application is based. Accordingly, in this study we have estimated a set of numbers comprising the Lake number, the Wedderburn and Burger numbers, and inflow and outflow Froude numbers. Therefore we have used two years worth of time series data (2000-2001) consisting of temperature profiles, morphometry data, meteorological data, and inflow and withdrawal data of two reservoir located in the Mediterranean region.

Key Words: Hydrodynamic., Reservoir regime

Introduction

The understanding of lake hydrodynamics has made much progress in the last twenty years. However, it is still difficult for the general limnological practitioner to gain a quantitative description of the hydrodynamical regimes in a particular lake at a particular time (Imberger, J. (1994))

In general hydraulics characterisation of flow is based essentially on the Reynolds and Froude numbers. So flows are subdivided into laminar or turbulent and super or sub-critical. Therefore, an analogy methodology may be established to permit the limnologist to classify hydrodynamic regime in lakes. Such hydrodynamical regime is important because the mixing and transport process operating in a lake determine, to a large degree, the ecological response of the lake to meteorological forcing, inflows and outflows. Thus, one-dimensional model like the DYRESM is applied to a Mediterranean reservoir such as the Sau or Boadella, it is important to check the validity of assumptions on which its application is based. Accordingly, in this study we have estimated a set of numbers comprising the Lake number, the Wedderburn and Burger numbers, and inflow and outflow Froude numbers. For both reservoirs, we have used two years worth of time series data (2000-2001) consisting of temperature profiles, morphometry data, meteorological data, and inflow and withdrawal data. The temperature profiles have been converted to density profiles using the UNESCO (1981) state formula equation. Later, we have used these density profiles to calculate the non-dimensional numbers. Lake Number

The Lake number L_N is a dimensionless parameter defined as the ratio of the moments of the stabilizing force of gravity. This. L_N describes the water upwelling from the hypolimnion to the surface layer, expressed by the equation:

$$L_{N} = \frac{\left(Z_{g} - Z_{o}\right)Mg\left(1 - \frac{Z_{T}}{Z_{H}}\right)}{A^{3/2}\left(1 - \frac{Z_{g}}{Z_{H}}\right)\rho_{0}.u_{*}^{2}}$$
(1.1)

where Z_0 is the centre of gravity of the water mass and Z_g is the centre of volume for the entire lake body; Z_T is the height to the centre of the metalimnion; Z_H is the depth from the bottom

of the reservoir; M is the total mass of water [Kg]; g is acceleration due to gravity $[m.s^{-2}]$; ρ_0 is the average water density $[kg.m^{-3}]$; A is the surface area of the reservoir A(Z); and u_* is the water friction velocity $[m.s^{-1}]$.

 Z_0 and Z_s are defined respectively as follows:

$$Z_{0} = \frac{\sum_{i=0}^{Z_{ii}} \rho_{i}(Z_{i}) Z_{i} . A(Z_{i})}{\sum_{i=0}^{Z_{m}} \rho_{i}(Z_{i}) A(Z_{i})}$$
(12)

$$Z_{g} = \frac{\sum_{i=0}^{Z_{n}} Z_{i} \cdot A(Z_{i})}{\sum_{i=0}^{Z_{n}} \cdot A(Z_{i})}$$
(1.3)

$$u_*^2 = \frac{\rho_a}{\rho_o} C_D U_{10}^2 \tag{1.4}$$

where U_{10} is the wind velocity at 10 m above the water surface $[m.s^{-1}]$; C_D is the drag coefficient = 1.3.10⁻³ [dimensionless]; and $\frac{\rho_a}{\rho_0}$ is the ratio between air and water densities = 1.2.10⁻³

[dimensionless].

Under these circumstances, the isopycnals are expected to be primarily horizontal and little seiching of the seasonal thermocline or turbulent mixing in the hypolimnion are expected. For $L_N \ll 1$, stratification is weak with respect to wind stress. Under these circumstances, the seasonal thermocline is expected to experience strong seiching and the hypolimnion is expected to experience extensive turbulent mixing due to internal shear (Imberger 1989). Thus the hypolimnion water, very rich in nutrients, will reach the surface layer during the wind episode (Imberger 2001).

Wedderburn Number

The Wedderburn number represents the ratio of the baroclinic restoring force to the wind disturbance force, or the ratio of the restoring moment about the centre of the volume of the lake to the disturbance moment. W describes the upwelling of water from the metalimnion into the water surface, expressed by:

where g' is the modified acceleration due to gravity across the uppermost thermocline.

$$W = \frac{g'h^2}{u_*^2.L}$$
(1.5)

This is represented by $g = \frac{\Delta \rho}{\rho_o} g$, where $\Delta \rho$ is the density difference between the surface

layer and the mean water density, and h is the depth of the diurnal thermocline; u_* is the water shear velocity due to wind stress and approximated by the bulk aerodynamic formula as previously defined in the Lake number calculation; and L is the length of the lake.

e. For W >> 1, tilting of the isotherms due to applied wind stress will be small and horizontal variations negligible. This coincides with strong stratification, light winds, and slow deepening of the mixed layer. For W << 1, deepening is dominated by internal shear production and will occur over a much shorter time scale than horizontal convection in the surface layer (Imberger & Patterson 1990). Where W is small and L_N large, only the upper region of the thermocline will respond to wind forcing. Where W and L_N are small, the lake as a whole should respond, and vertical mixing should occur throughout it (Imberger and Patterson 1990).

Burger Number

The Burger number S_i is an indicator of the influence of the earth's rotation on water motion in reservoirs; influence on the water internal waves. S_i is expressed by:

$$S_i = \frac{c_i}{L_w f} \tag{1.6}$$

where L_w is the width of the reservoir and $\frac{c_i}{f}$ is the Rossby radius; C_i is the wave velocity

expressed by:

$$c_i = \sqrt{g'H} \tag{1.7}$$

 $g = g \cdot \frac{\Delta \rho}{\rho_0}$ is the reduced gravity; $\Delta \rho$ is the difference between surface water and mean H is the

mean reservoir water depth, which depends on the inflow entering the reservoir and water withdrawal from the reservoir. f is the Coriolis parameter equal to the double rate of rotation of the earth at the latitude of the lake, $S_i = 1$ is the critical value indicating that the rotation is of the same magnitude as gravity. When $S_i >> 1$, the internal oscillations increasingly take on the characteristics of simple gravitational seiches (Antenucci & Imberger 2001).

When $S_i \ll 1$, the waves have characteristics similar to those of an inertial oscillation, with the majority of the energy in the wave being in the form of kinetic energy.

Inflow Froude number

The regime behaviour of the river inflow entering the reservoir is described by the inflow Froude number, $F_{\rm ri}$

$$\frac{h_i}{H} = \left[\frac{Q_i}{g_i^{1/2} H^{3/2} . L_w}\right]^{2/3} = F_{ri}^{2/3}$$
(1.8)

where Q_i is the peak inflow discharge; H is the total depth of the reservoir; $g'_i = \frac{\Delta \rho}{\rho 0}$ is the

reduced gravity; $\Delta \rho$ is the difference between inflowing water density and the mean reservoir water

density; ρ_0 is the mean water density; and Fri = 1 is the critical value of the plunge or rise. Where $F_{r_i} >> 1$, the inflow is too large to separate as an underflow or an overflow. When $F_{r_i} << 1$, the inflow separates as an underflow or an overflow. Once it has been established that the river water underflows ($\Delta \rho_i > 1$ and hi/H<1), it is necessary to carry out a more detailed analysis to estimate its entrainment into the downflow and thus the depth of the inflow intrusion.

Outflow Froude number

The outflow Froude number characterises the type of water withdrawal, expressed by the equation:

$$F_{r_0} = \left[\frac{Q_0}{g^{1/2}H^{5/2}}\right]$$
(1.9)

where Q_0 is the outflow discharge; $g' = \frac{\Delta \rho}{\rho 0}$ is the reduced gravity; $\Delta \rho$ is the difference

between outflow water density and the mean reservoir water density; ρ_0 is the mean water density; H is the total depth of the reservoir. Where $F_{r_0} \ll 1$, then the outflow is selective from a depth corresponding to the outflow level.

Methods

Lake numbers were computed for each recorded temperature profile using equation 1.1. We used twenty measured over two years (2000-2001) for the Sau Reservoir and fifteen for the Boadella

Reservoir. As water depth decreases and increases with water inflow and outflow, the water surface and the reservoir volume change. To calculate both, interpolation from the bathymetric data was necessary. To determine the daily velocity friction we used equation 2.4, with a drag coefficient of $1.3.10^{-3}$, and a ratio between air and water densities of $1.2.10^{-3}$. Wind velocity is given in meteorological data in Fig. 2.8 for the Sau Reservoir and in Fig. 2.21 Chapter 2 for the Boadella Reservoir. The mean water density was taken as $1000 kg.m^{-3}$. The depth of the reservoir Z_{H} and its area were estimated using morphometry data (Sections 2.4.1 and 2.5.1, Chapter 2). The estimated lake numbers are 712 in Sau reservoir and 636 in Boadella Reservoir

As described above for lake number, Wedderburn number values were estimated by linear interpolation between existing profiles. For each temperature profile using equation 1.5 daily friction velocity u_* had been previously defined in the calculation of the Lake number.

Modified acceleration due to gravity g' is the ratio of the difference in diurnal thermocline density from the mean water density, divided by the mean water density multiplied by gravity g. L is the average length of the reservoir: L = 3000m for Sau and L = 1500m for Boadella.

The Burger number was obtained using equation 1.6 in which the Rossby radius was calculated as the ratio between longwave phase velocity and inertial frequency.

Longwave phase speed is a function of reduced gravity g', which depends on the difference between surface water density and mean water density divided by the mean reservoir water density. Inertial frequency depends on the latitude of a reservoir; the Sau and Boadella reservoirs are located in the same region and have approximately the same altitude.

The inflow Froude number was calculated using equation 1.8. The discharge or inflow rate Q_i is the peak inflow discharge entering the reservoir and was estimated from the inflow file: approximately $217m^3 \cdot s^{-1}$ for the Sau Reservoir and $111 \cdot m^3 \cdot s^{-1}$ for Boadella The reduced gravity g'_{1} is the difference between inflow density and mean reservoir density divided by the mean density. The average width of the reservoir is B = 700m for Sau and 600m for Boadella. The total depth of the reservoir H is variable, depending on the volume entering and leaving it.

The outflow Froude number was computed using equation 1.9. The outflow Q_0 was deduced from the withdrawal data. The reduced gravity for outflow is the ratio of the outflow density minus the mean water density to the mean water density. H is the reservoir water depth. **Results and discussions**

Lake number

The L_N values obtained for the Sau Reservoir corresponding to lowest wind velocity 0.8m/s and the minimum is around 2 approximately in the middle of December 2001. Thus, $L_N > 1$ indicating that stratification is the dominant force when compared to wind stress. Minimum and maximum wind velocities are 0.8 and 2.9(m/s) respectively. There is low turbulence and no mixing in deeper water, due to the isolation of the bottom waters from the surface. Consequently, However at the end of 2001 the Lake number was equal 2, indicating that the hypolimnion was relatively mixed.

The L_{N} of the Boadella Reservoir fluctuated from a minimum value of 5 in the beginning of June 2000 corresponding relatively to high wind velocity 5.6m/s (see section 2.5.2.4 Chapter 2) to a maximum of 2226 in the end of Mars 2000 corresponding to the lowest wind velocity 0.4 m/s. Compared to Sau the stratification is strong in the first year (2000) and during the second (2001). This is linked to low wind velocity, for which minimum value and maximum values are 0.8 and 2.9 for Sau and 0.7 and 2.1 for Boadella (see Figs. 2.8 and 2.21, Chapter 2.) It should also be noted that morphometry plays an important role in the determination of Lake number, and that determination of the thermocline is difficult. In both reservoirs, water upwelling from the hypolimnetic occurs at the winter end autumn in 2000 and 2001. Fig 1.1 shows the differences in Sau and Boadella's Lake numbers. In this figure we see that lake number diminished corresponding to the peak inflow (see Fig. 2.10B, Chapter 2) in the end of the year 2000 means that may inflow also contribute in hypolimnion mixing.

However, in Boadella Reservoir the lack of profiles from the end of August until the end of April influence the estimation of lake number for comparison purposes versus inflow. Also, withdrawal being selective may enhance stratification. For both reservoirs through the period 2000 to 2001 Lake numbers are bigger than the critical value. This indicates that stratification is relatively strong and that the deepest part of the hypolimnion remains unmixed if not influenced by inflow/outflow and cooling forces. Unfortunately, there are fewer profiles for Boadella than there are for Sau. However, the variation in its Lake number is small, as is the case for Sau. Also, it should be noted that the wind velocity in Boadella, on the days when profiles were taken, was relatively low. We can therefore conclude that both reservoirs were not completely mixed, at least at the time the profiles were taken. It has should also be noted, however, that the profiles were taken during the day. In winter, during the day, and the mean velocity of the wind is in general not high enough to overcome stratification. For example, on 09/02/2000:

 $Z_g - Z_0 = 1.6.10^{-3} m$, $u^* = 0.0017 m s^{-1}$ and $L_N = 60$. However, it is very likely that at night time $Z_g - Z_0$ was close to 0 and L_N went to 0. In these circumstances hypolimnetic mixing could be expected.



Fig 1.1 The differences in the Sau and Boadella Lake numbers

Wedderburn number

The Wedderburn numbers in the Sau Reservoir do change substantially, tending to oscillate over the two years between 0 and 750. Only one value is below 1 corresponding to the value in the beginning of November 2000 corresponding to the high wind velocity 5.6 m/s. 0, indicating that wind stress on the surface of the lake is able to overcome the stratification in the water column and metalimnetic water can be expected to be vented into the surface layer if we neglect other disturbing forces such as inflow/outflow and cooling.

Wedderburn numbers in the Boadella Reservoir range from approximately 0 to 454 at the end of May and are smaller than those of Sau, See Fig. 1.2 for Sau and Boadella Wedderburn number differences.



Figure 1.2 Sau and Boadella Wedderburn numbers

Burger number

The Sau Reservoir experiences substantial fluctuation in Si values throughout the two years, with all the values above 1. Burger numbers range from 1.20 to 2.3, with a mean value of approximately 1.75. both constant. The Burger number is high than the critical value 1.0 and therefore the rotational effects are insignificant. However, given that Si is close to 1, rotation would be discarded. The Sau and Boadella Burger numbers are shown in Fig.1.3



Figure 1.3 Comparison between the Sau and Boadella Burger numbers. Sau is represented by squares, and Boadella by circles.

Inflow Froude number

The average Sau inflow Froude number is 0.01.. It is important to note that it would be necessary to carry out a more detailed analysis to estimate the entrainment into the inflow and the depth of the downflow insertion.

The inflow Froude number for Boadella is smaller for Sau. Arnera rivers which flow into Boadella. Fig.1.4 shows the inflow Froude numbers for Sau and Boadella.



Figure 1.4 Sau and Boadella inflow Froude numbers

Outflow Froude number

Sau's average outflow Froude number is about 0.01, which is lower than the critical value of 1.0. Boadella's average outflow Froude number is 0.001, ten times smaller than Sau's one. This indicates that in both reservoirs the outflow is selective. Fig. 1.5 shows the Sau and Boadella outflow Froude numbers.



Figure 1.5 Sau and Boadella outflow Froude numbers

Conclusions

The Lake number L_N while the Wedderburn number W is an indicator of surface layer mixing. In both reservoirs, L_N is large and W is small for the profiles under study. This means that

the the one-dimensional DYRESM model can be used. (Imbeger, J. 2001). Where $L_N \prec 1$, It should be pointed out, however, that to calculate the L_N we have used daily mean wind taken during the daytime. It is likely that there are times during the night and/or when there are very high winds that $L_N \prec 0$, Wedderburn number are not enough because it leads to an overestimation of these numbers especially when the days when profiles were taken are calm therefore daily temperature profiles and daily inflow are needed to judge perfectly whether the one dimensional hydrodynamic may be applied or not. For this reason, daily lake numbers, which were obtained by interpolation of daily temperature from monthly observed water temperature profiles, , density structure is approximately horizontal and the one dimensional assumption is valid. Also we have estimate the daily wedderburn number as we did for lake numbers. Wedderburn numbers, are mostly greater than one indicating that tilting of the isotherms is small; this is due to the weakness of the wind stress.

The Burger number S_i is slightly larger than one, indicating that rotation might be discarded.

 $F_{r_i} \ll 1$ and $F_{r_o} \ll 1$ indicate that in both reservoirs separation occurs

References:

Afres, W and L. Andreas. 2003. Small-scale Hydrodynamic in lakes Ann.Rev.Fluid Mech. 35: 373-412.

Amborosetti, W and L. Barbanti. 2001. Temperature, heat content, mixing and stability in Lake Orta: a pluriannual investigation. Limnol. 60(1): 60-68.

Ambrosetti, W., L.Barbanti and N. Sala. 2003. Residence time and physical processes in lakes. Limnol. 62(Suppl. 1): 1-15.

Aminot, A. And R. Kérouel. 2004. Dissolved organic carbon, nitrogen and phosphorus in the N-E Atlantic and the N-W Mediterranean with particular reference to non-refractory fractions and degradation. Deep-Sea Research. I 51: 1975-1999.

Amrosetti, W and L. Barbanti. 2002. Physical limnology of Italian lakes. 1. Relationship between morphometry and heat content. Limnol. **61**(2): 147-157.

Andradóttir, H. Ó and H. M. Nepf. 2000. Thermal mediation by littoral wetland and impact on lake intrusion depth. Water Ressources Research. **36**(3): 725-735.

Andrew, J. Tanentzap, D. P. Hamilton, and N. D. Yan. 2007. Calibrating the Dynamic Reservoir Simulation Model (DYRESM) and filling required data gaps for one-dimensional thermal profile predictions in a boreal lake. Limnol. Oceanogr.Methods. **5**: 484–494.

Antenucci, J. P and J. Imberger. 2003. The seasonal evolution of wind/internal wave resonance in Lake Kinneret Limnol. Oceanogr. **48**(5): 2055-2061.

Antenucci, J and A. Imerito. 2003 The CWR Dynamic Reservoir Simulation Model DYRESM. User Manual. Centre for Water Research. University of Western Australia.

Antenucci, J., and A. Imerito. 2002 The CWR Dynamic Reservoir Simulation Model DYRESM. Science Manual. Centre for Water Research. University of Western Australia.

Appt, J., J. Imberger, and H. Kobus. 2004. Basin-scale motion in stratified upper Lake Constance. Limnol.Oceanogr. **49**(3): 919-933.

Armengol, J., J. Toja, J., and A. Vidal. 1994. Seasonal rhythm and secular changes in Spanish reservoirs. In "Limnology Now: A Paradigm of Planetary Problems." (R. Margalef, ed.)

Armengol, J., M. Comerma, J.C. Gracía, M. Romero, J.J. Rodriguez and A. Vidal 1999. Contribució al coneixement de l'ecologia acuática de l'embassament de Sau evoluciò de l'embassament al 1998. Aigües Ter de Llobregat. pp 66

Armengol, J., M. Comerma, J.C. Gracía, M. Romero, J.J. Rodriguez and A. Vidal 2000. Contribució al coneixement de l'ecologia acuática de l'embassament de Sau evoluciò de l'embassament al 1999. Aigües Ter de Llobregat. pp 118.

Armengol, J., J. Gracia, M. Comerma, M. Romero, J. Dolz, M. Roura, B. P. Han, A. Vidal and K. Simek. 1999. Longitudinal Processes in Canyon Type Reservoirs: The Case of Sau (N.E. Spain). Theoretical Reservoir Ecology and its Applications 313-345.

Bruce, L. C., D Hamilton, J. Imberger, G. Gal, M. Gophen, T. Zohary and K. D. Hambright. 2006 A numerical simulation of the role of zooplankton in C, N and P cycling in Lake Kinneret, Israel. Ecological Modelling.193. 412-436.

Carr, G. M., H.C. Duthie and W.D. Taylor. 1997. Models of aquatic plant productivity: a review of the factors that influence growth. Aquatic Botany. 59 195-215.

Casmitjana, X., T. Serra, J. Colomer, C. Baserba and J. Pérez-Losada. 2003. Effects of the water withdrawal in the stratification patters of a reservoir. Hydrobiologia. 504: 21-28.

Casamitjana, X., T. Serra, M. Soler, J. Colomer. 2002. A study of the evolution of the particle boundary layer in a reservoir, using laser particle sizing. Water Research 36: 4293-4300.

Chan, T. U., D. P. Hamilton, B J. Robson, B. R, Hodges and Chris. Dallimore. 2002. Impacts of hydrological Changes on Phytoplankton Succession in the Swan River, Western Australia. Estuaries. 25(68): 1406-1415.

Colomer, J., T. Serra, M. Soler and X. Casamitjana. 2002. Sediment fluidization events in a lake caused by large monthly rainfalls Geophysical research Letters. 29, 0.1029/2001GL014299

Colomer, J., T. Serra, M. Soler, X. Casamitjana. 2003. Hydrothermal plumes trapped by thermal stratification Geophysical Research Letters 30(21): 2092,

Colomer, J., E. Roget and X. Casamitjana 1996. Daytime heat balance for estimating non-radiative fluxes of lake Banyoles, Spain. Hydrological Processes. 10: 721-726.

Comerma, M., J. C. Garc, M. Romero, J. Armengol, K. Šimek.2003. Carbon flow dynamics in the pelagic community of the Sau Reservoir (Catalonia, NE Spain). Hydrobiologia 504: 87-98.

Dallimore, C. J., J. Imberger and B. R. Hodges. 2004 Modeling a Plunging Underflow Journal of Hydraulic Engineering. **130**(11): 1068-1076.

Dallimore, C. J., B. R. Hodges and J. Imberger. 2003 Coupling an Underflow

Model to a Three-Dimensional Hydrodynamic Model. Journal of Hydraulic Engineering, ABCE. **748** Ewing, T., T.R. Romero, J. Imberger, J. Antenucci and A. Deen. 2004. A real-time reservoir decision support system. (6th International conference on Hydro informatics World) scientific publishing Company, ISBN 981-238-787-0

Fernandes, R. L and J. Imberger. 2006. Bed roughness induced entrainment in a high Richardson number underflow. Journal of Hydraulic Research. **44**(6): 725-738.

Fischer, J. 1979. Modelling of water quality processes in lakes and reservoirs. Hydrological Sciences. 24: 2-6.

Fleenor, W. E. 2001. Effects and Control of Plunging Inflows on Reservoir Hydrodynamics and Downstream Releases PhD thesis pp 160

Fleenor, W. E. 2001. Effects and Control of Plunging Inflows on Reservoir Hydrodynamics and Downstream Releases PhD thesis pp 160

Fricker, P.D and H.M. Nepf. 2000. Bathymetry, stratification, and internal seiche structure Journal of Geophysical research **105** (6) 14237-14251.

Fu, S. and B. R. Hodges. 2005. The Grid Scale Problem in Numerical Modeling of Flow Around Large Woody Debris in Rivers. University of Texas at Austin Graduate Student Research Conference. April 28, 2005

Fu, S. and B. R. Hodges. 2005. The Grid Scale Problem in Numerical Modeling of Flow Around

Gal, G., J. Imberger, T. Zohary, J. P. Antenucci, A. Anis, and T. Rosenberg. 2003. Simulating the thermal dynamics of Lake Kinneret. Ecological Modelling. **162**(1-2): 69-86.

Hodges, B. R and S. K. Delavan. 2004. Numerical Diffusion in Hydrostatic Models of Internal Waves. 17th ASCE Engineering Mechanics Conference, June 13-16, 2204, University of Delaware, Newark, DE, EM.

Hodges, B. R., J. Imberger, B. Laval and J. Appt. 2000. Modelling the Hydrodynamics of Stratified Lakes. Hydroinformatics 2000 Conference, Iowa Institute of Hydraulic Research, 23-27.

Hurtado, J. V. Basin-Scale Hydrodynamics in a Mediterranean reservoir. Implications for the phytoplankton dynamics. PhD Theses. University of Girona. 133 pp.

Imberger, J. 2001. Characterizing the dynamical regimes of a lake 6th Workshop on physical Process in Natural Waters University of Girona: 77-92

Yeates. P.S., J. Imberger. 2003. Pseudo two-dimensional simulations of internal and boundary fluxes in stratified lakes and reservoirs. Intl.J.River Basin Management. IAHR and INBO. **1** (4). 297-319.